

Column design

Rectangular columns · EN 1992-1-1 §5.8, §6.1, §9.5 · UK NA / PN-EN

Reference	NAE-RC-008 · version 1.0
Standards	BS EN 1992-1-1:2004 with UK NA · PN-EN 1992-1-1:2008 with Polish NA (NDP sources listed on the NDP sheet)
National Annex	Selectable: UK NA to BS EN 1992-1-1 or Polish NA to PN-EN 1992-1-1
Issued	30 October 2026

What it does

Ultimate limit state design of a rectangular reinforced concrete column under an axial force and a bending moment about one axis: slenderness, imperfections, second order effects by the nominal curvature method, and the resistance from an N-M interaction curve worked out by strain compatibility, with the detailing rules for columns.

How to use

1. Open the Calculation sheet and select the National Annex.
2. Fill in the shaded input cells. Everything else is calculated.
3. Read the Results block; every step below it quotes its clause. Print or save as PDF for your calculation package.

Scope and limitations

Rectangular section, bars of one size symmetrical about both axes: n_b bars on each face parallel to b and n_h bars (corners included) on each face parallel to h . Bending about one axis, with h in the plane of bending; check the other axis with a second copy (swap b with h and n_b with n_h , and enter the moments, bracing and effective length of that axis) and biaxial bending to 5.8.9 separately. End moments only: loads between the ends of the column are outside the scope. Compression only ($N_{Ed} > 0$). The aspect ratio b/h or h/b is at most 4 (9.5.1). Isolated member: imperfection $\theta_i = \theta_0 \alpha_h$ with $\theta_0 = 1/200$ and $\alpha_m = 1$ (5.2(5), (6)). Slenderness limit from (5.13N) with A , B and C from the inputs; effective length l_0 from the user (5.8.3.2). Second order moment by nominal curvature (5.8.8) with $c = 10$, or 8 for a constant first order moment (5.8.8.2(4)). The entered end moments exclude imperfections: the imperfection moment $N_{Ed} e_i$ is added at both ends in the direction of M_{02} ; where it is not smaller than M_{02} the moments are taken as due to imperfections and $C = 0.7$. Resistance by strain compatibility: parabola-rectangle concrete of 3.1.7(1) with the strain limits of 6.1(5) (0.0035 at the compressed face, 0.002 at $3h/7$ once the whole section is compressed), bars elastic-plastic, the concrete displaced by the bars deducted; M_{Rd} at N_{Ed} by bisection on the strain state (60 steps). Concrete classes up to C50/60, $f_{yk} \leq 500$ MPa. Link spacing to 9.5.3; the 0.6 reduction near beams, slabs and laps is the user's to apply.

The second-generation EN 1992-1-1:2023 is not yet implemented.

Further reading and independent cross-check

- The Concrete Centre, How to design concrete structures using Eurocode 2: Columns.
 - The Concrete Centre, Worked Examples to Eurocode 2: Volume 1.
 - The Concrete Centre, RC Spreadsheets v4, TCC53 Column design (licensed product) can be used as an independent cross-check.
- NA Engineering is not affiliated with The Concrete Centre or CIRIA; their publications are referenced for information only.

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Disclaimer

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Revision history

v1.0	30 Oct 2026 · First issue
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Project
Element
Date

Job no.
Made by
Checked

Inputs · section

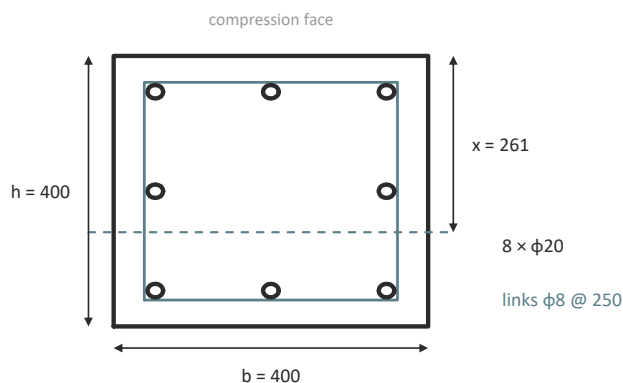
Shaded cells only

	National Annex		UK NA (BS EN)	
Table 3.1	Concrete strength class		C32/40	
3.2.2	Reinforcement characteristic yield strength (≤ 500 MPa)	f_{yk}	500	MPa
8.2(2)	Maximum aggregate size	d_g	20	mm
	Section width (perpendicular to the plane of bending)	b	400	mm
	Section depth (in the plane of bending)	h	400	mm
4.4.1	Nominal cover to links	c_{nom}	35	mm
	Link diameter	φ_w	8	mm
9.5.3	Link spacing	s_w	250	mm
9.5.3(6)	Cross-ties on the intermediate bars		Corner bars only	
9.5.2(1)	Bar diameter	φ	20	mm
	Bars on each face parallel to b (top and bottom)	n_b	3	
	Bars on each face parallel to h (corners included)	n_h	3	

Inputs · actions and length

ULS design values

	Design axial force (compression)	N_{Ed}	1800	kN
5.8.8.2(2)	Larger first order end moment M02	M_{02}	60.0	kNm
5.8.8.2(2)	Smaller end moment M01 (negative in double curvature)	M_{01}	20.0	kNm
5.8.3.1	Bracing		Braced	
5.2(5)	Clear height of the column (for αh)	l	5000	mm
5.8.3.2	Effective length	l_0	4250	mm
5.8.4	Effective creep ratio	φ_{ef}	1.50	
5.8.8.2(4)	Curvature factor (10; 8 for a constant moment)	c	10	
	Inputs valid and consistent			OK

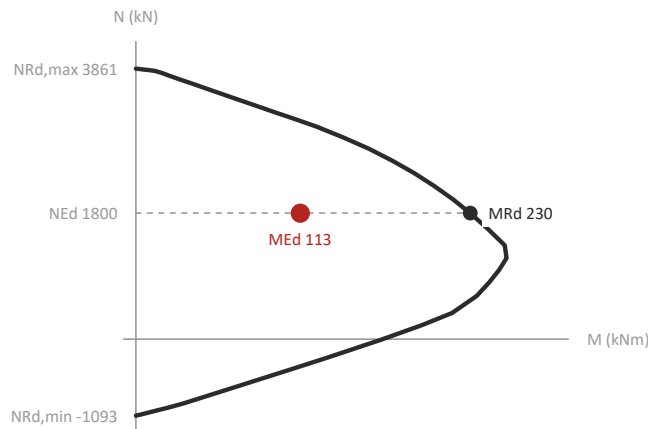
Your section, to scale · compression face on top · neutral axis at the resistance for N_{Ed} (dashed)


Results

Bending at N_{Ed} M_{Ed} / M_{Rd}	0.49	OK
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Axial force $N_{Ed} / N_{Rd,max}$		0.47		OK
Design moment (with second order effects when slender)	M_{Ed}	113.0	kNm	! Slender
Detailing (bar size, areas, spacing, links) · As provided	A_s	2513	mm ²	OK

N-M interaction curve · design point (red) · resistance at N_{Ed}



Calculation · materials and section

2.4.2.4(1)	Partial factor, concrete	γ_c	1.50		NDP sheet
2.4.2.4(1)	Partial factor, reinforcement	γ_s	1.15		NDP sheet
3.1.6(1)	Coefficient on compressive strength (flexure)	α_{cc}	0.85		NDP sheet
9.5.2(1)	Minimum diameter of longitudinal bars	φ_{min}	12	mm	NDP sheet
Table 3.1	Characteristic cylinder strength	f_{ck}	32	MPa	
Table 3.1	Mean tensile strength	f_{ctm}	3.02	MPa	
3.1.6(1)	Design compressive strength $\alpha_{cc} f_{ck} / \gamma_c$ ($\eta = 1$)	f_{cd}	18.13	MPa	
3.2.7	Design yield strength	f_{yd}	434.8	MPa	
3.2.7(4)	Modulus of elasticity of reinforcement	E_s	200000	MPa	
	Gross area $b h$	A_c	160000	mm ²	
	Number of bars $2 n_b + 2 (n_h - 2)$	n	8		
	Reinforcement area	A_s	2513	mm ²	
	Centre of the corner bars from the face $c + \phi_w + \phi/2$	d_1	53	mm	
5.8.8.3(2)	Radius of gyration of the bars about the centroid	i_s	127.3	mm	
	Mechanical reinforcement ratio $A_s f_{yd} / (A_c f_{cd})$	ω	0.377		
(5.13N)	Relative axial force $N_{Ed} / (A_c f_{cd})$	n	0.620		

Calculation · slenderness and design moment

5.8.3.2	Radius of gyration $h / \sqrt{12}$	i	115.5	mm	
(5.14)	Slenderness l_0 / i	λ	36.8		
(5.13N)	$A = 1 / (1 + 0.2 \phi_e f)$	A	0.769		
(5.13N)	$B = \sqrt{1 + 2\omega}$	B	1.324		
(5.13N)	Moment ratio M_{01} / M_{02}	r_m	0.333		
(5.13N)	$C = 1.7 - r_m$ (braced); 0.7 unbraced or $M_{02} \leq N_{Ed} e_i$ (imperfect)	C	1.367		
(5.13N)	Slenderness limit $20 A B C / \sqrt{n}$	λ_{lim}	35.3		
5.2(5)	$\alpha h = 2 / \sqrt{l}$, $2/3 \leq \alpha h \leq 1$ (l in m)	α_h	0.894		
(5.1)	Inclination $\theta_i = \theta_0 \alpha h \alpha_m$, $\theta_0 = 1/200$, $\alpha_m = 1$	ϑ_i	0.00447		
(5.2)	Eccentricity from imperfections $\theta_i l_0 / 2$	e_i	9.5	mm	
5.8.8.2(2)	End moments with imperfections $M_{02} + N_{Ed} e_i$	$M_{02'}$	77.1	kNm	
5.8.8.2(2)	$M_{01} + N_{Ed} e_i$	$M_{01'}$	37.1	kNm	
6.1(4)	Minimum eccentricity $\max(h / 30; 20 \text{ mm})$	e_o	20.0	mm	

(5.36)	$K_r = (n_u - n) / (n_u - n_{bal}) \leq 1, n_u = 1 + \omega, n_{bal} = 0.4$	K_r	0.774	
(5.37)	$\beta = 0.35 + f_{ck}/200 - \lambda/150$	β	0.265	
(5.37)	$K_{\phi} = 1 + \beta \phi_{ef} \geq 1$	K_{ϕ}	1.397	
5.8.8.3(2)	Effective depth $h/2 + i_s$	d	327.3	mm
(5.34)	Curvature $K_r K_{\phi} \epsilon_{yd} / (0.45 d)$	$1/r$	1.60E-05	1/mm
(5.33)	Second order eccentricity $(1/r) l_0^2 / c$	e_2	28.8	mm
(5.31)	Second order moment $N E d e_2$ (slender columns only)	M_2	51.9	kNm
(5.32)	Equivalent first order moment $0.6 M_{02} + 0.4 M_{01} \geq 0.4 M_{02}$	M_{0e}	61.1	kNm
5.8.8.2	Design moment $\max(M_{0e} + M_2; M_{02}; M_{01} + M_2/2; N E d e_0)$	M_{Ed}	113.0	kNm

Calculation · resistance (see the Interaction sheet)

6.1(5)	Axial resistance in compression (uniform strain $\epsilon_{c2} = 0.002$)	$N_{Rd,max}$	3861	kN	
6.1	Axial resistance in tension $-A_s f_{yd}$	$N_{Rd,min}$	-1093	kN	
	Largest sampled moment on the curve (scale of the chart)	M_{max}	255.1	kNm	
6.1	Neutral axis depth with $N = N_{Ed}$ (bisection, Interaction sheet)	x	261	mm	
6.1	Axial force at that depth (check: = N_{Ed})	N	1800.0	kN	
6.1	Moment resistance at N_{Ed}	M_{Rd}	230.0	kNm	
6.1	Axial force $N_{Ed} \leq N_{Rd,max}$	N_{Ed}	1800	kN	OK
6.1	Moment $M_{Ed} \leq M_{Rd}$	M_{Ed}	113.0	kNm	OK

Calculation · detailing (9.5)

(9.12N)	Minimum reinforcement $\max(0.10 N_{Ed} / f_{yd}; 0.002 A_c)$	$A_{s,min}$	414	mm ²	
9.5.2(3)	Maximum reinforcement $0.04 A_c$ (outside laps)	$A_{s,max}$	6400	mm ²	
8.2(2)	Minimum clear gap $\max(\phi; d_g + 5; 20)$	a_{min}	25	mm	
	Clear gap along b $(b - 2d_1)/(n_b - 1) - \phi$	a_b	127	mm	
	Clear gap along h $(h - 2d_1)/(n_h - 1) - \phi$	a_h	127	mm	
9.5.3(1)	Minimum link diameter $\max(6; \phi / 4)$	$\phi_{w,min}$	6.0	mm	
9.5.3(3)	Maximum link spacing $\min(20 \phi; b; h; 400)$	$s_{cl,tmax}$	400	mm	
9.5.3(6)	Largest clear distance from a free bar to a restrained bar	s_{free}	127	mm	Corners and tied bars restrained
(9.12N)	Reinforcement $A_s \geq A_{s,min}$	A_s	2513	mm ²	OK
9.5.2(3)	Reinforcement $A_s \leq A_{s,max}$	A_s	2513	mm ²	OK
9.5.2(1)	Bar diameter $\phi \geq \phi_{min}$	ϕ	20	mm	OK
8.2(2)	Clear gaps $\min(a_b; a_h) \geq a_{min}$		127	mm	OK
9.5.3(1)	Link diameter $\phi_w \geq \phi_{w,min}$	ϕ_w	8	mm	OK
9.5.3(3)	Link spacing $s \leq s_{cl,tmax}$	s	250	mm	OK
9.5.3(6)	Every bar within 150 mm of a restrained bar	s_{free}	127	mm	OK

Not in the detailing status: reduce the link spacing by 0.6 within a distance equal to the larger dimension of the column above and below a beam or slab, and at laps of bars over 14 mm, with at least three links in the lap length (9.5.3(4)). ϕ_{min} : UK NA 12 mm, PL NA.6 6 mm.

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N-M interaction · strain compatibility, EN 1992-1-1 §6.1

Parabola-rectangle of 3.1.7(1), (3.17): $\epsilon_{c2} = 0.002$, $\epsilon_{cu2} = 0.0035$, $n = 2$, $f_{cd} = \alpha_{cc} f_{ck} / \gamma_c$, no tension. Strain limits of 6.1(5), Fig. 6.1: 0.0035 at the compressed face while $x \leq h$; once the whole section is compressed, 0.002 at $3h/7$ from that face, down to the uniform 0.002. Bars elastic-plastic, $E_s = 200$ GPa, horizontal branch (3.2.7(2)b); the concrete displaced by the bars is deducted at the concrete stress at each bar centre. z_c : depth in compression, $\min(x, h)$. M about the centroid of the gross section, compression positive.

	x (mm)	z _c (mm)	N (kN)	M (kNm)
1	tension	0	-1092.7	0.0
2	4	4	-1069.2	4.7
3	12	12	-1022.3	13.7
4	20	20	-975.3	22.5
5	30	30	-916.6	33.0
6	40	40	-662.5	71.8
7	50	50	-429.0	107.0
8	60	60	-259.9	132.3
9	80	80	-4.8	169.2
10	100	100	197.7	196.4
11	120	120	372.9	217.6
12	140	140	616.5	234.5
13	160	160	812.4	243.3
14	180	180	991.0	250.2
15	200	200	1157.3	255.1
16	220	220	1340.3	253.9
17	240	240	1575.4	242.1
18	260	260	1792.7	230.4
19	280	280	1996.0	218.3
20	300	300	2188.0	205.4
21	320	320	2370.9	191.6
22	340	340	2546.1	176.7
23	360	360	2712.9	160.8
24	380	380	2873.7	143.6
25	400	400	3030.5	124.9
26	420	400	3140.1	109.5
27	440	400	3227.8	97.2
28	480	400	3358.5	78.9
29	540	400	3486.2	61.0
30	600	400	3568.4	49.6
31	700	400	3653.6	37.7
32	800	400	3705.4	30.5
33	1000	400	3764.0	22.5
34	1200	400	3795.7	18.1
35	1600	400	3827.1	13.4
36	2400	400	3842.5	8.1
37	4000	400	3851.6	4.5
38	10000	400	3857.9	1.7
39	uniform	400	3861.1	0.0

The table draws the curve. MRd at NEd below: bisection on the strain state s (0 to 1: $x = s h$; 1 to 2: $t = 2 - s$, whole section compressed

step	s low	s high	x (mm)	zc (mm)	N (kN)	M (kNm)
1	0.000000	2.000000	400.0	400.0	3030.5	124.9
2	0.000000	1.000000	200.0	200.0	1157.3	255.1
3	0.500000	1.000000	300.0	300.0	2188.0	205.4
4	0.500000	0.750000	250.0	250.0	1686.0	236.3
5	0.625000	0.750000	275.0	275.0	1946.4	221.4
6	0.625000	0.687500	262.5	262.5	1818.8	228.9
7	0.625000	0.656250	256.3	256.3	1753.1	232.6
8	0.640625	0.656250	259.4	259.4	1786.2	230.8
9	0.648438	0.656250	260.9	260.9	1802.6	229.8
10	0.648438	0.652344	260.2	260.2	1794.4	230.3
11	0.650391	0.652344	260.5	260.5	1798.5	230.1
12	0.651367	0.652344	260.7	260.7	1800.5	230.0
13	0.651367	0.651855	260.6	260.6	1799.5	230.0
14	0.651611	0.651855	260.7	260.7	1800.0	230.0
15	0.651733	0.651855	260.7	260.7	1800.3	230.0
16	0.651733	0.651794	260.7	260.7	1800.1	230.0
17	0.651733	0.651764	260.7	260.7	1800.1	230.0
18	0.651733	0.651749	260.7	260.7	1800.0	230.0
19	0.651733	0.651741	260.7	260.7	1800.0	230.0
20	0.651733	0.651737	260.7	260.7	1800.0	230.0
21	0.651733	0.651735	260.7	260.7	1800.0	230.0
22	0.651733	0.651734	260.7	260.7	1800.0	230.0
23	0.651734	0.651734	260.7	260.7	1800.0	230.0
24	0.651734	0.651734	260.7	260.7	1800.0	230.0
25	0.651734	0.651734	260.7	260.7	1800.0	230.0
26	0.651734	0.651734	260.7	260.7	1800.0	230.0
27	0.651734	0.651734	260.7	260.7	1800.0	230.0
28	0.651734	0.651734	260.7	260.7	1800.0	230.0
29	0.651734	0.651734	260.7	260.7	1800.0	230.0
30	0.651734	0.651734	260.7	260.7	1800.0	230.0
31	0.651734	0.651734	260.7	260.7	1800.0	230.0
32	0.651734	0.651734	260.7	260.7	1800.0	230.0
33	0.651734	0.651734	260.7	260.7	1800.0	230.0
34	0.651734	0.651734	260.7	260.7	1800.0	230.0
35	0.651734	0.651734	260.7	260.7	1800.0	230.0
36	0.651734	0.651734	260.7	260.7	1800.0	230.0
37	0.651734	0.651734	260.7	260.7	1800.0	230.0
38	0.651734	0.651734	260.7	260.7	1800.0	230.0
39	0.651734	0.651734	260.7	260.7	1800.0	230.0
40	0.651734	0.651734	260.7	260.7	1800.0	230.0
41	0.651734	0.651734	260.7	260.7	1800.0	230.0
42	0.651734	0.651734	260.7	260.7	1800.0	230.0
43	0.651734	0.651734	260.7	260.7	1800.0	230.0
44	0.651734	0.651734	260.7	260.7	1800.0	230.0
45	0.651734	0.651734	260.7	260.7	1800.0	230.0
46	0.651734	0.651734	260.7	260.7	1800.0	230.0
47	0.651734	0.651734	260.7	260.7	1800.0	230.0
48	0.651734	0.651734	260.7	260.7	1800.0	230.0
49	0.651734	0.651734	260.7	260.7	1800.0	230.0

50	0.651734	0.651734	260.7	260.7	1800.0	230.0
51	0.651734	0.651734	260.7	260.7	1800.0	230.0
52	0.651734	0.651734	260.7	260.7	1800.0	230.0
53	0.651734	0.651734	260.7	260.7	1800.0	230.0
54	0.651734	0.651734	260.7	260.7	1800.0	230.0
55	0.651734	0.651734	260.7	260.7	1800.0	230.0
56	0.651734	0.651734	260.7	260.7	1800.0	230.0
57	0.651734	0.651734	260.7	260.7	1800.0	230.0
58	0.651734	0.651734	260.7	260.7	1800.0	230.0
59	0.651734	0.651734	260.7	260.7	1800.0	230.0
60	0.651734	0.651734	260.7	260.7	1800.0	230.0

Nationally Determined Parameters

Values used by the Calculation sheet for the selected National Annex. Sources: UK NA to BS EN 1992-1-1:2004, Table NA.1; PN-EN 1992-1-1:2008, Załącznik krajowy NA. Edit only if your project specifies different values.

Parameter	Clause	UK NA	PL NA	Notes
Partial factor, concrete γ_c	2.4.2.4(1)	1.5	1.4	Persistent & transient. UK NA: recommended; PL: NA.2, Table NA.2
Partial factor, reinforcement γ_s	2.4.2.4(1)	1.15	1.15	UK NA: recommended; PL: NA.2, Table NA.2
α_{cc} (compression in flexure / axial)	3.1.6(1)	0.85	1	UK NA: 0.85; PL: recommended (NA.9)
$\alpha_{cc,pl}$ (plain concrete, compression)	12.3.1(1)	0.6	0.8	UK NA Table NA.1: 0.6; PL: recommended (NA.9)
α_{cc} (shear and punching)	3.1.6(1)	1	1	UK NA: 1.0 for other phenomena; PL: recommended (NA.9)
α_{ct} (design tensile strength)	3.1.6(2)	1	1	Recommended value in both annexes
CRd,c numerator (CRd,c = value / γ_c)	6.2.2(1), 6.4.4(1)	0.18	0.18	Recommended value in both annexes
k1 (axial stress term, punching)	6.4.4(1)	0.1	0.1	Recommended value in both annexes
vRd,max factor (vRd,max = factor · v · fcd)	6.4.5(3)	0.5	0.4	UK NA: 0.5 v fcd; PL: recommended value (NA.9), 0.4 v fcd since EN 1992-1-1 AC:2010 (PN-EN 1992-1-1:2008)
kmax (vEd ≤ kmax · vRd,c at u1)	6.4.5	2	1.5	UK NA 6.4.5(3): 2 vRd,c. PL: no limit in PN-EN 1992-1-1:2008; 1.5 (A1:2014 recommendation) applied conse
ϕ_{large} (large bar threshold, mm)	8.8(1)	40	32	UK NA: 40 mm; PL: 32 mm recommended (NA.9)
cot θ upper limit (variable strut)	6.2.3(2)	2.5	2	UK NA: 2.5 (1.25 with axial tension); PL: NA.4, $1 \leq \cot \theta \leq 2.0$
k1 (x/d limit, $\delta \geq k1 + k2 x_u/d$)	5.5(4)	0.4	0.44	UK NA for $f_{yk} \leq 500$ MPa; PL: recommended (NA.9)
k2 (x/d limit, $\epsilon_{cu2} = 0.0035$)	5.5(4)	1	1.25	UK NA: $0.6 + 0.0014/\epsilon_{cu2}$; PL: $1.25(0.6 + 0.0014/\epsilon_{cu2})$
Upper limit on the (310/ σ_s) factor (0 = none)	7.4.2(2)	1.5	0	UK NA Table NA.5 Note 5: (310/ σ_s) or (500/ f_{yk})($A_s,prov/A_s,req$) ≤ 1.5; PL: none
L/d not to exceed 40 K (1 = applies)	7.4.2(2)	1	0	UK NA Table NA.5 Note 6; not in EN text
ϕ_{min} (longitudinal bars in columns, mm)	9.5.2(1)	12	6	UK NA: 12 mm; PL: NA.6, 6 mm
k3 (crack spacing)	7.3.4(3)	3.4	3.4	Recommended value in both annexes
k4 (crack spacing)	7.3.4(3)	0.425	0.425	Recommended value in both annexes
k1 (concrete stress, characteristic; XD, XF, XS)	7.2(2)	0.6	1	UK NA: recommended; PL: NA.5, $k1 = 1.0$
k2 (concrete stress, quasi-permanent; linear cr)	7.2(3)	0.45	0.45	Recommended value in both annexes (UK NA; PL NA.9)
k3 (steel stress, characteristic)	7.2(5)	0.8	0.8	Recommended value in both annexes (UK NA; PL NA.9)
k4 (steel stress, imposed deformation)	7.2(5)	1	1	Recommended value in both annexes (UK NA; PL NA.9)